



# Measurement and Data

## Hello!!!

**1 per Sticky Note - Put on board**

What are 3 things you find challenging about teaching measurement and/or data?

Karen Hensen  
Resource Teacher  
CRMC  
Columbus State University

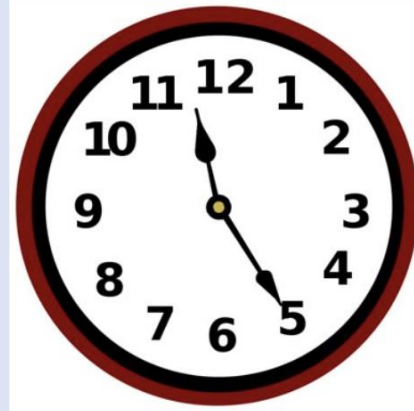


# WODB

A



B



C



D



# Connections

## Domains

- Counting and Cardinality
- Operations and Algebra
- Numbers and Base Ten/  
Fractions
- Measurement (other areas)
- Geometry

A clock can be divided into 4 equal parts or quarters.

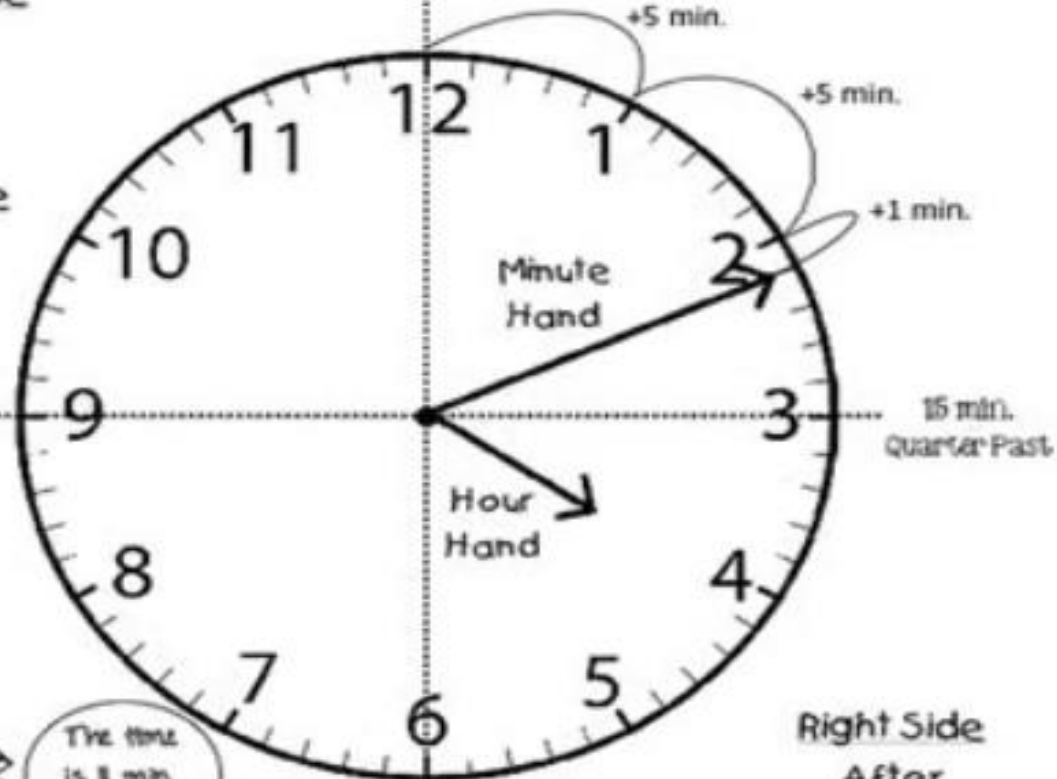
O'clock  
60 min. = 1 Hour

Midnight begins A.M.  
Noon begins P.M.

Left Side

Till  
Until  
To  
Before

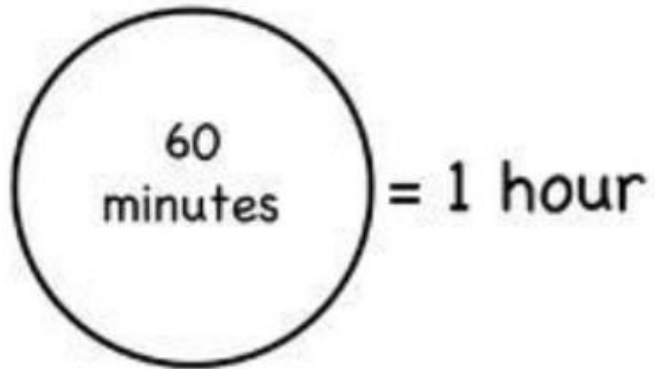
45 min.  
Quarter Till



The time is 15 min. past 4.

30 Minutes  
One Half Hour  
Half Past

# Connections



$1/2$  hour



half past

$1/4$  hour



quarter to  
quarter after

## Domains

- Counting and Cardinality
- Operations and Algebra
- Numbers and Base Ten/  
Fractions
- Measurement (other areas)
- **Geometry**

# What is elapsed time?

I tell my students a guest speaker will be coming in, in 30 minutes. When will he arrive?



**STOP!**  
Make them look at the clock and figure it out!

## Domains

- Counting and Cardinality
- Operations and Algebra
- Numbers and Base Ten/  
Fractions
- Measurement (other areas)
- Geometry



We left the house at 9:05 for an appointment.  
We were running late by about 15 minutes.  
What time were we suppose to leave to get to  
our appointment on time?

What time was it 15 minutes ago?



Notice?  
Wonder?

groups



How many professional learning hours will you receive for this workshop?

**Session**

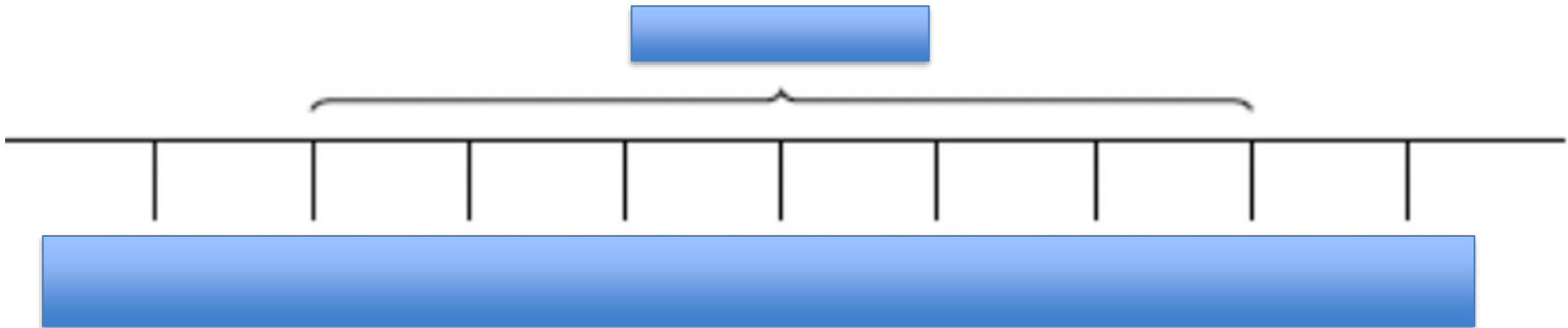
8:30 - 3:00

Lunch 11:30 – 12:30

# Time

## Number Line Diagram

- Easier
- Consider movement of the hour and minute hands



*What time does Marla have to leave to be at her friend's house by a quarter after 3 if the trip takes 90 minutes?*



Do

## Elapsed time on the number line

Maria started reading at 3:30. She read for 1 hour and 15 minutes. At what time did Maria stop reading? Use a number line to find out.



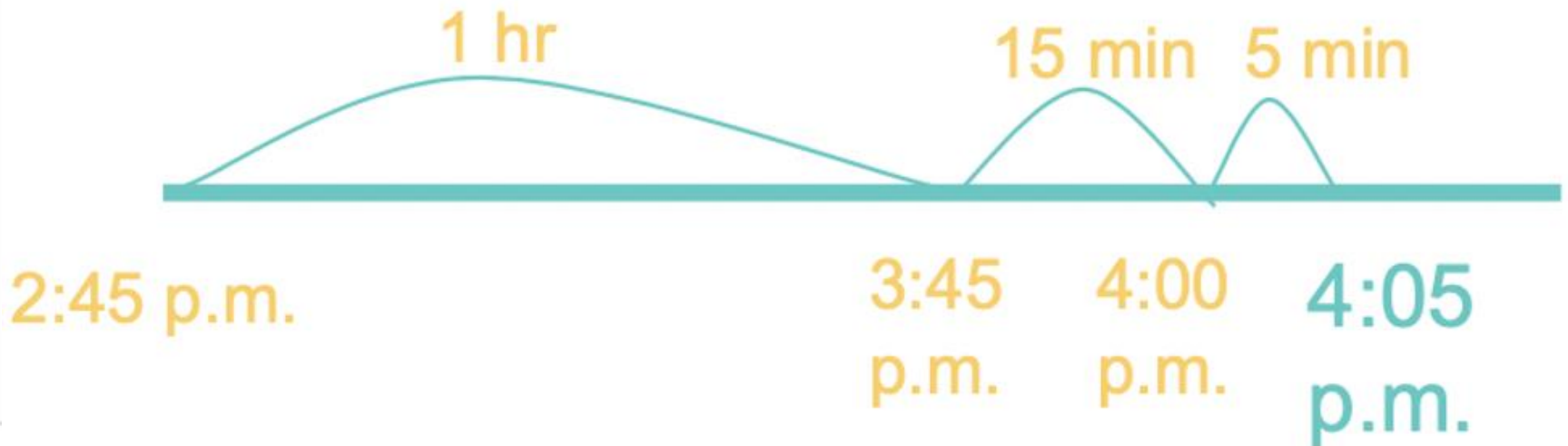
Maria stopped reading at .

# Connection

## Domains

- Counting and Cardinality
- Operations and Algebra
- Measurement and Data

A movie began at 2:45p.m. and lasted 1 hr. and 20 min. What time was it when the movie over?



# Connections

Domains

1 hr = 60 min.

8

77

~~9 hrs 17 min~~

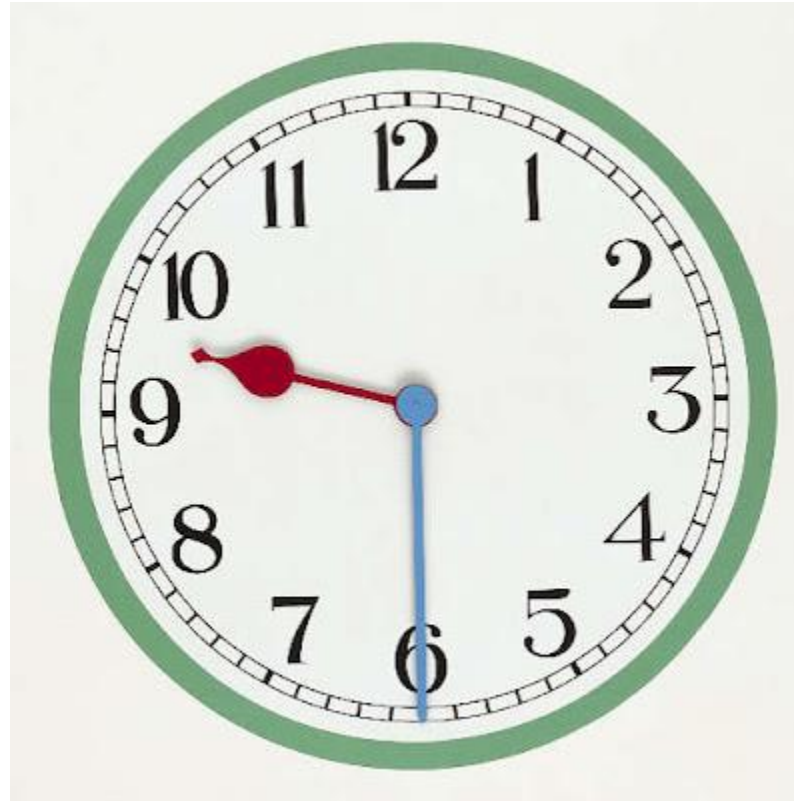
~~- 7 hrs 30 min~~

1 hr 47 min

On holiday, we are driving from Columbus, GA to Virginia Beach. We are all tired because we have been in the car for 7 ½ hrs. According to our GPS (Global Positioning System) the trip will take 9 hrs. 17 min. How much longer do we have to endure being in the car?



# Break 10 minutes



- ★ Snacks and drinks
- ★ Restroom? Bottle Filling Station?
- To the right at the end of hall.



# 3 Act Tasks <https://gfletchy.com/3-act-lessons/>

**I SUPPORT TEACHERS AND STUDENTS IN DEVELOPING A CONCEPTUAL UNDERSTANDING OF MATH THROUGH INNOVATIVE IDEAS AND ENGAGING TASKS.**

Building Fact  
Fluency Toolkit



Build Fluency  
through Context  
and Purposeful  
Practice.

Problem Based  
Lessons



Problem-based  
lessons that will  
foster students'  
curiosity.

Progression  
Videos



Short videos that  
show content  
across grade  
levels.

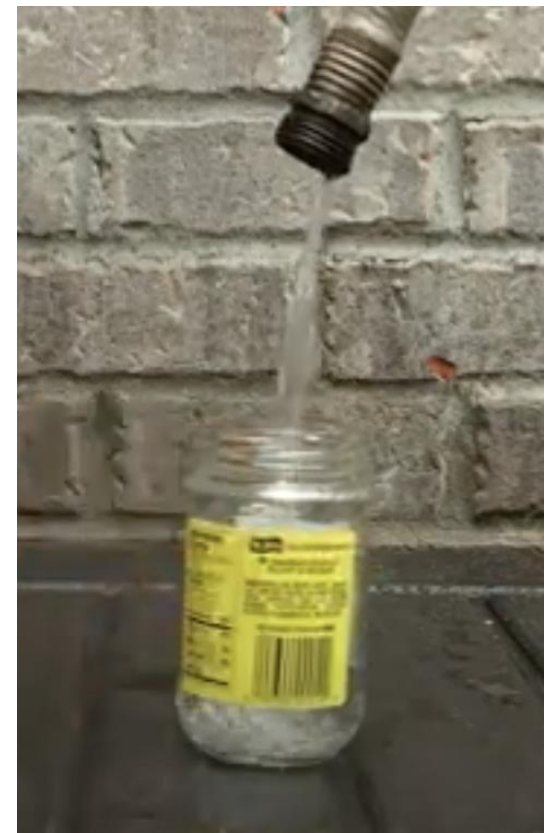
Online  
Workshops



Learn more  
about Graham's  
workshops

# Act 1

- What do you notice? wonder?
- How long will it take to fill up the 4 pickle jars? Estimate
- Write an estimate you know is too high and too low.



<https://youtu.be/OqJez7-ai-A>

# Act 2

Name: \_\_\_\_\_

<https://gfletchy.com/dill-er-up/>

1. What did you notice?	2. What do you wonder?
3. Main Question: How long will it take to fill up the 4 pickle jars?	
4. Estimate:	5. What information do you need?
6. Show your thinking:	

How long to fill up the small jar

Size of the small pickle jar

Size of the 4 jars

# Act 3

Name: \_\_\_\_\_

<https://gfletchy.com/dill-er-up/>

Wait to play the reveal

1. What did you notice?

2. What do you wonder?

3. Main Question:

How long will it take to fill up the 4 pickle jars?

4. Estimate:

5. What information do you need?

6. Show your thinking:





# Would you Rather...

Have Cheez-It's<sup>®</sup> to cover a rectangle with..

**A length of 9 and  
a perimeter of 22**



**A length of 5 and  
a perimeter of 20**

# FOOTBALL



# HOW MANY BLADES OF GRASS ARE ON A FOOTBALL FIELD?

WHY ask this question?  
Who would want/need  
to know this?

Ask a question  
and then collect  
data

School Area

# Van de Walle's Approach

- ground students' data analysis in a real-world context that is relevant and engaging for them
- encourage them to interpret data meaningfully, helping them develop an understanding of data concepts in a hands-on, practical way

- **Estimation strategies**
- **Multiplication**
- **Measurement**
- **Problem solving**
- **Communication**

- **Science**
- **Language Arts**
  - **Writing**

# Attributes

The first and most critical goal is for students to understand the attribute they are going to measure.

Van de Walle

- Measurable attributes are quantifiable characteristics of objects or events.
- What is the measurable attribute we are looking for?



HOW MANY BLADES OF GRASS ARE ON A FOOTBALL FIELD?



**Googol** =  $10^{100}$

(not even a googol grains of sand are found on all the beaches in the world)



Millions Period			Thousands Period			Ones Period		
Millions			Thousands			Ones		
hundreds	tens	ones	hundreds	tens	ones	hundreds	tens	ones
6	5	0	0	8	4	9	7	0

**Before Estimation**

**PERIODS IN THE PLACE VALUE CHART**

**Duodecillions**

**Undecillions**

**Decillions**

**Nonillions**

**Octillions**

**Septillions**

**Sextillions**

**Quintillions**

**Quadrillions**

**Trillions**

**Billions**

**Millions**

**Thousands**

**Units**

# Collect Data

How are we going to determine how many pieces of grass are on the school's football field?

POSSIBLE TO COUNT  
THEM ALL?



HOW MANY  
BLADES OF GRASS  
ARE ON A  
FOOTBALL FIELD?

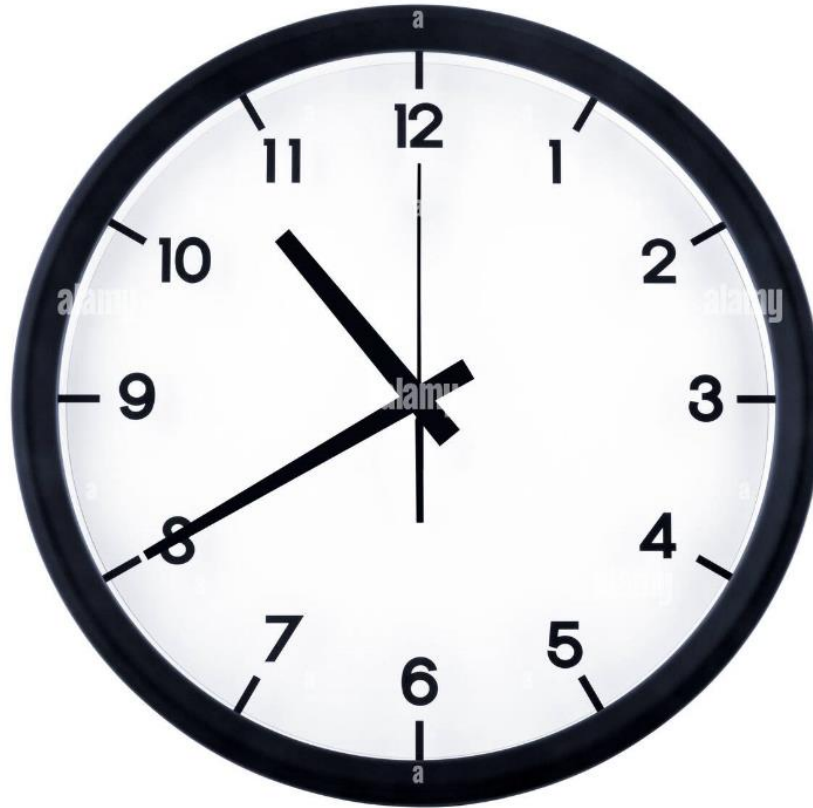
# Strategies to make a 'Good' Estimation

Good = close as we can get = **REASONABLENESS**





# Break 10 minutes



- ★ Snacks and drinks
- ★ Restroom? Bottle Filling Station?

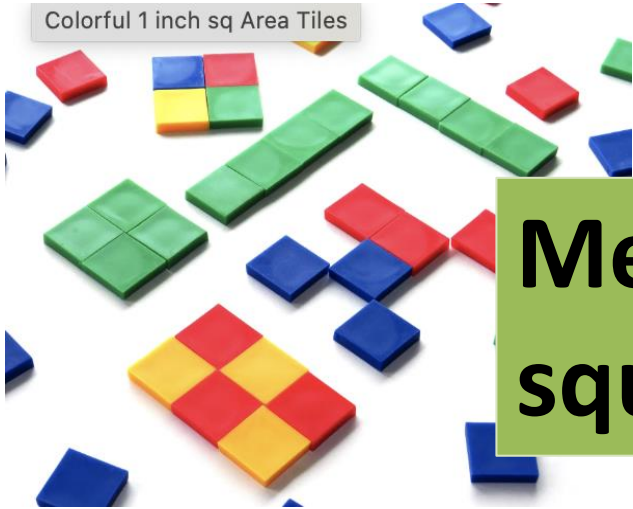


Do

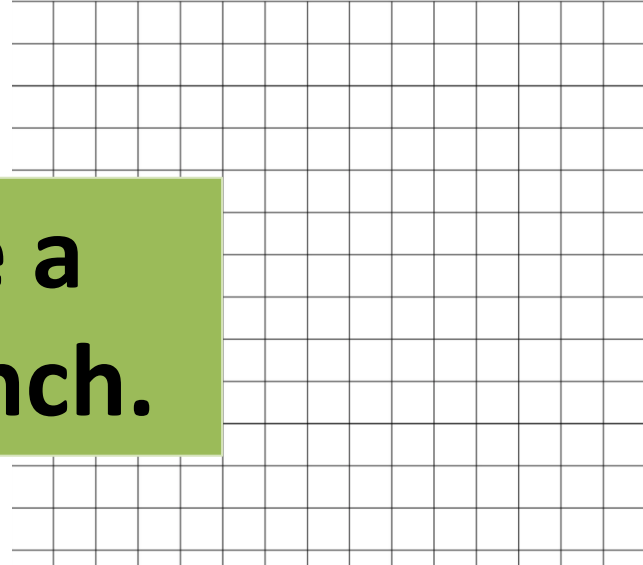
# Discover Area

## Square Tiles

Colorful 1 inch sq Area Tiles



## Graph Paper



**Measure a  
square inch.**

**Construct a model of a square foot.**

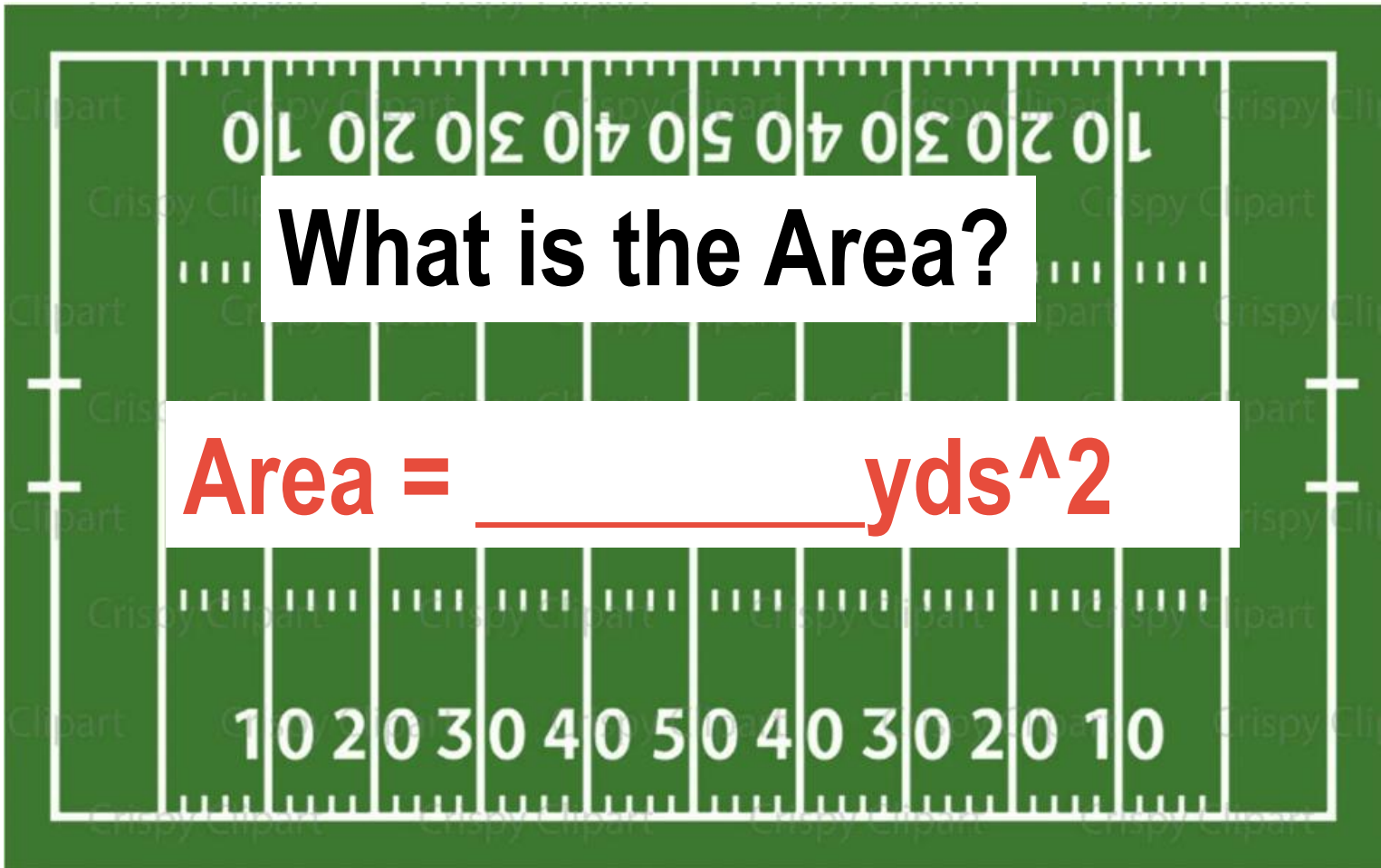
- square yard
- square meter

Do

# Dimensions: Tell/Discover

Length (known): **100 yards** (120yds)

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Width: **50 yards**



# Calculate Dimensions

## Length

1 foot (ft.) = 12 inches (in.)

1 yard (yd.) = 3 ft.

1 mile (mi.) = 1,760 yd.

1 mi. = 5,280 ft.

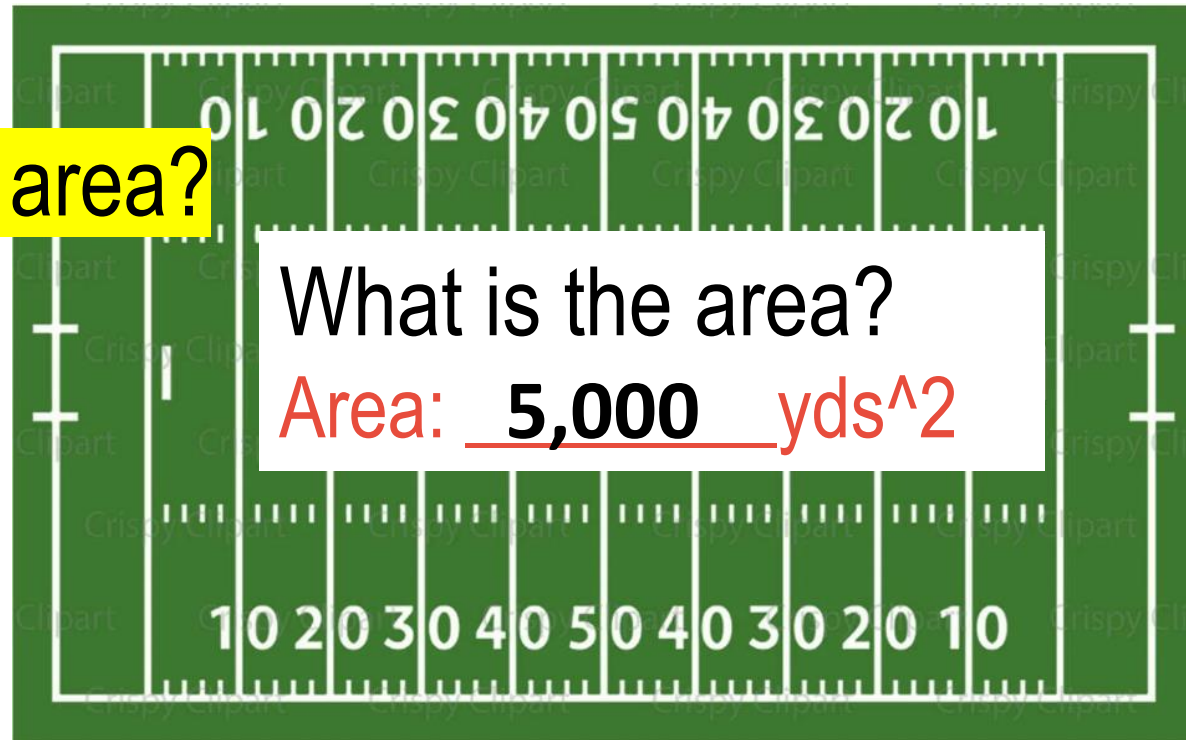
Length: 100 yds (playing field)

Width: 50 yds

How do we find the area?

$L \times W$

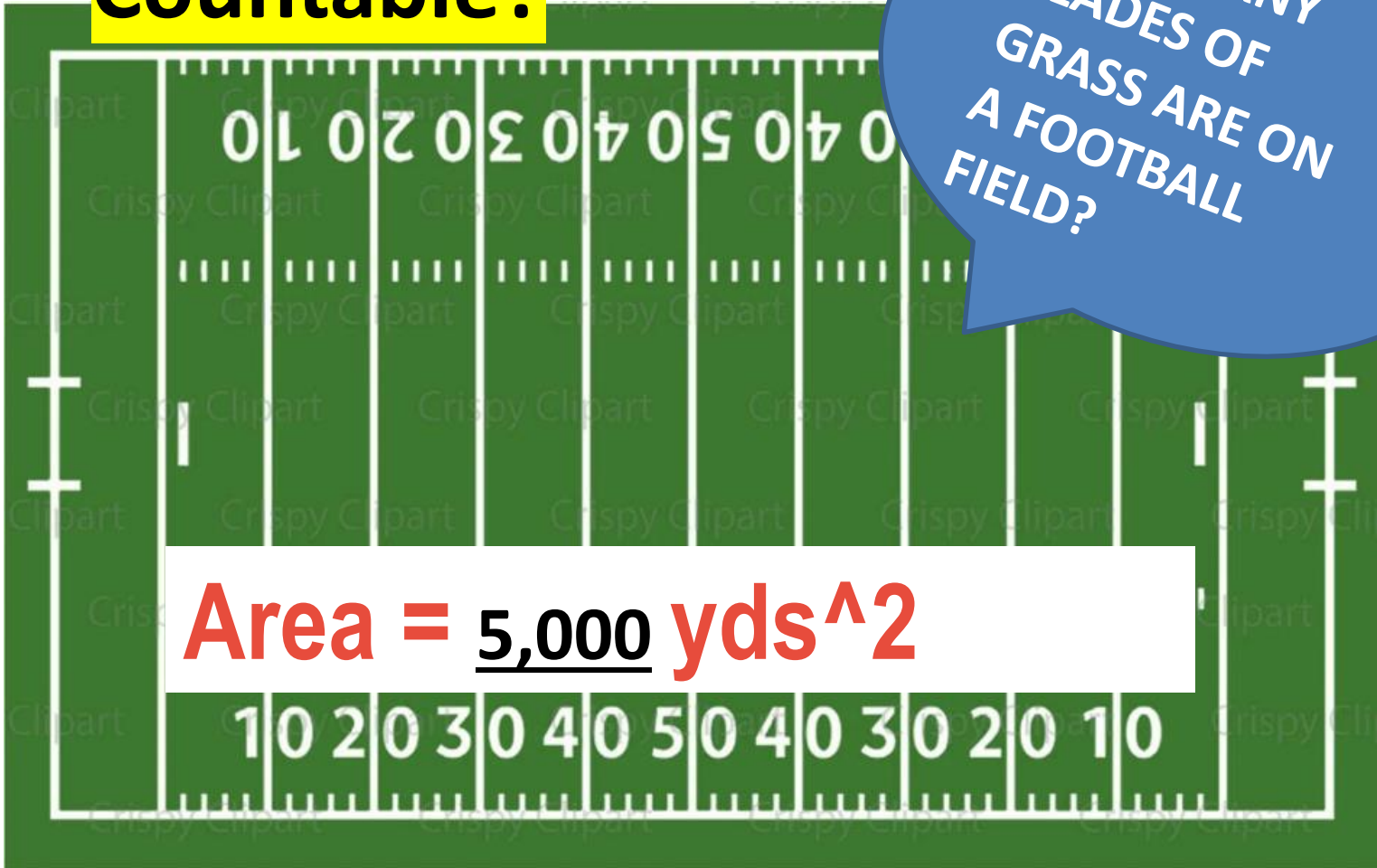
$100 \times 50$



# Grass Blades Countable?

HOW MANY  
BLADES OF  
GRASS ARE ON  
A FOOTBALL  
FIELD?

50 yards



100 yards

Do

# How Can We Collect the Data?

square inch frame



HOW MANY  
BLADES OF  
GRASS ARE ON A  
FOOTBALL FIELD?

- Put over the grass to count the blades.



chart

# Collecting & Recording Data

Group	Number of Blades



# Organize the Data

## Stem and Leaf Plots/Diagrams

- Stem and Leaf

A stem and leaf plot is a frequency diagram in which

1, 5, 12, 7, 22, 4, 5, 27, 3, 13, 19

Stem	Leaf
0	1 3 4 5 5 7
1	2 3 9
2	2 7

## Stem & Leaf plot



5 | 0 6 8

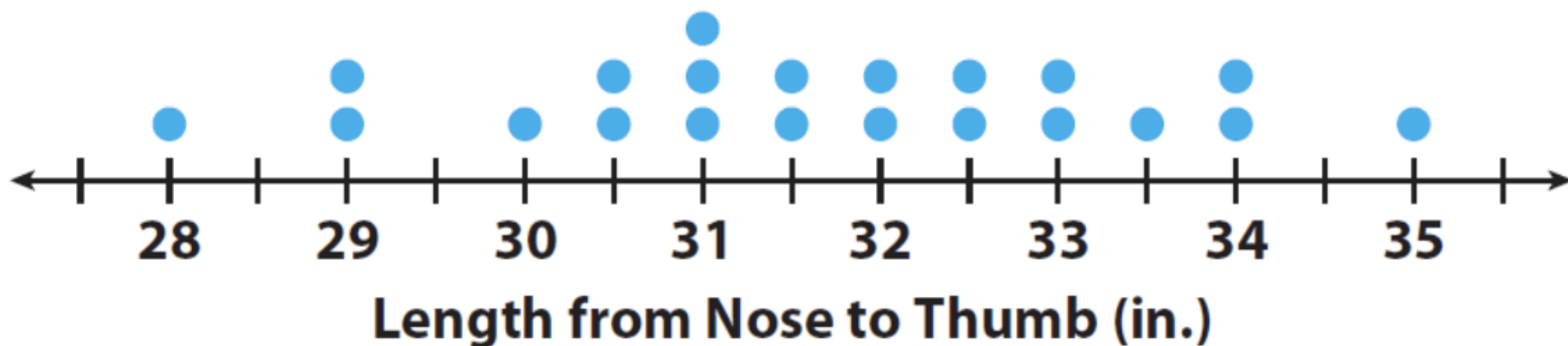
13<sup>th</sup> data value



chart

# Graph the Data

- Line Plot



chart

# Analyzing Data

Why the differences in count?

Range?

What number do we use?

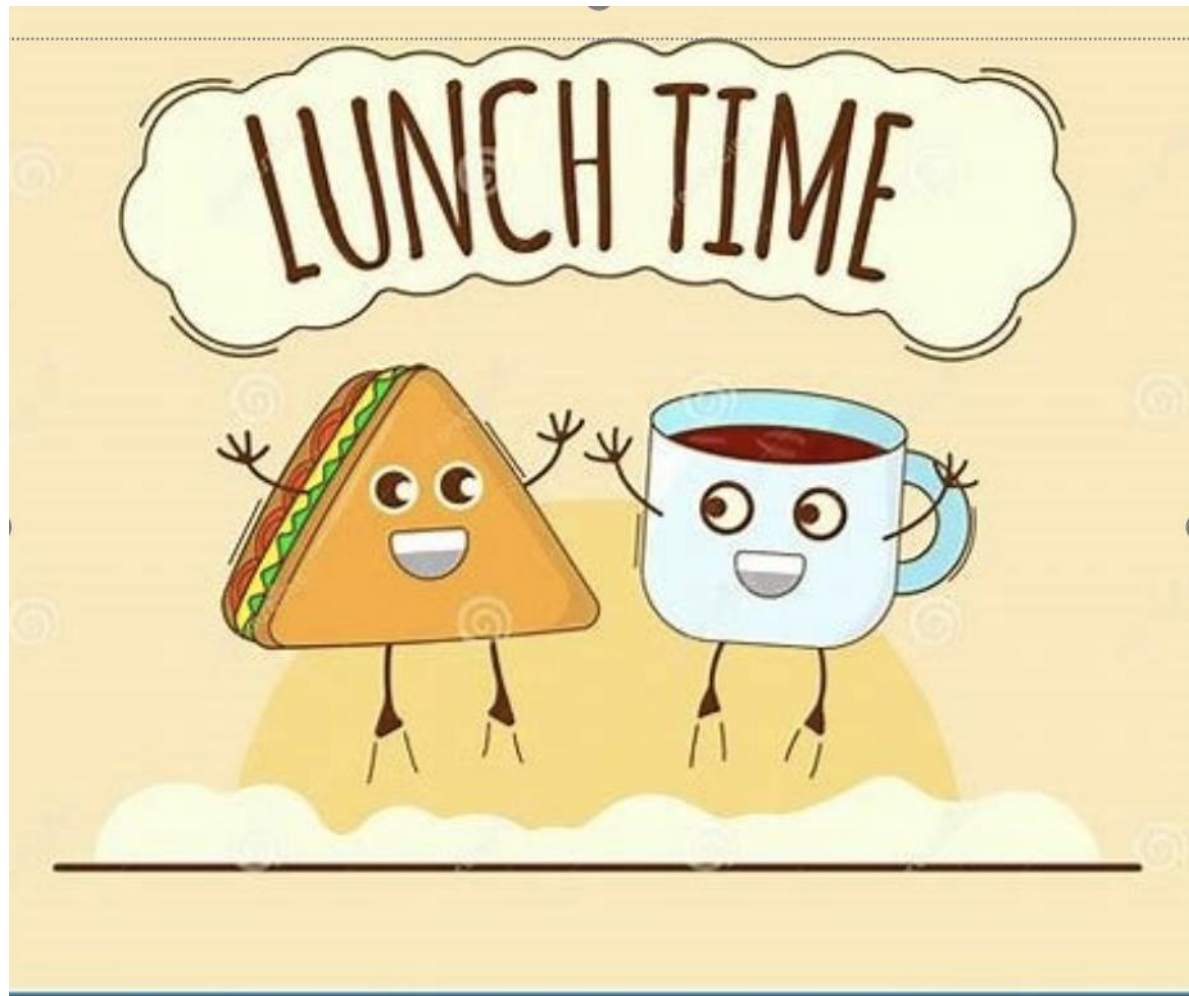
Averages:

Mean?

Median?

Mode?





**11:30 – 12:30**

Do

# Review Information

✓ Football field is  $5000 \text{ yd}^2$

✓ 1 sq. in. has \_\_\_\_\_ average blades of grass

## Length

1 foot (ft.) = 12 inches (in.)

1 yard (yd.) = 3 ft.

1 mile (mi.) = 1,760 yd.

1 mi. = 5,280 ft.

---

Now What?

How do we figure it out?

HOW MANY BLADES  
OF GRASS ARE ON A  
FOOTBALL FIELD?

# Calculate Dimensions

Length: 100 yds

Width: 50 yds

What is the Area?

Area: 5,000 yds<sup>2</sup>

15,000 ft<sup>2</sup>

180,000 in<sup>2</sup>

4,181 m<sup>2</sup>

## Length

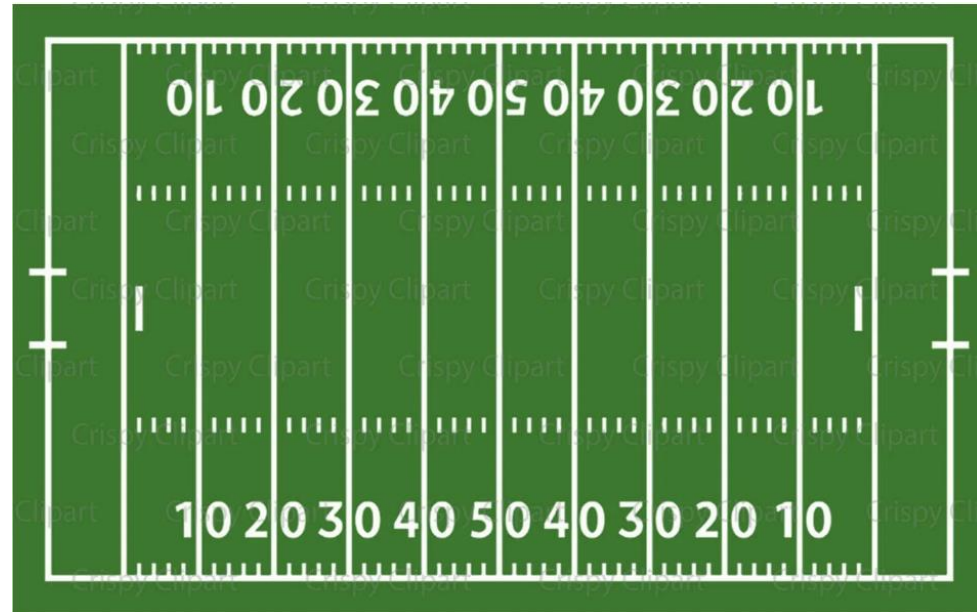
1 foot (ft.) = 12 inches (in.)

1 yard (yd.) = 3 ft.

1 mile (mi.) = 1,760 yd.

1 mi. = 5,280 ft.

1 yard = 0.914 meter



do

# Review Information

✓ Football field is 5000 yd<sup>2</sup>

✓ 1 sq. in. has \_\_\_\_\_ average blades of grass

HOW MANY  
BLADES OF  
GRASS ARE  
ON A FOOTBALL  
FIELD?

## ONE WAY

How many square inches  
are in a football field?

1 sq. ft. = 144 sq. in.

1 sq. yd = 1296 sq. in.

Now  
What?

### Length

1 foot (ft.) = 12 inches (in.)

1 yard (yd.) = 3 ft.

1 mile (mi.) = 1,760 yd.

1 mi. = 5,280 ft.

# Report - Share Findings

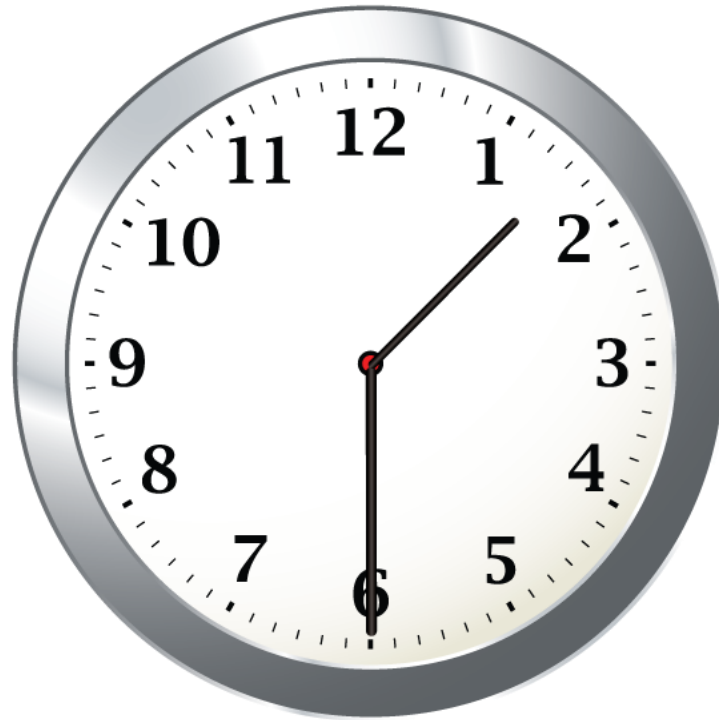
- Writing to explain mathematical thinking.
- Teach writing process!
- Write a letter to a football team/grounds keeper and tell what did and see what they say.
  - Who cares how many blades of grass are on a football field?
    - Groundskeepers (a small # of blades might indicate not doing job well)
    - Football players (types of shoes)

# Writing Process

- Explanation
  - Brainstorm the process to solve the problem
    - Individual
    - Large group
  - Match the steps of the process to with the reasons for those steps
  - Brainstorm whole group
  - Rough drafts
    - Include all steps
    - Reasons for choosing the steps
    - Pictures, diagrams that explain their thinking
    - Number sentences in explanations
  - Revise
    - Peer revise (groups of 3-4)
    - 1 criterion at a time using different colors
      - Number steps listed
      - Underline the whys
      - Circle number sentences
      - Circle picture/diagram
  - Teacher Writing conference based on rubric
  - Final draft
  - Mail



# Break 10 minutes



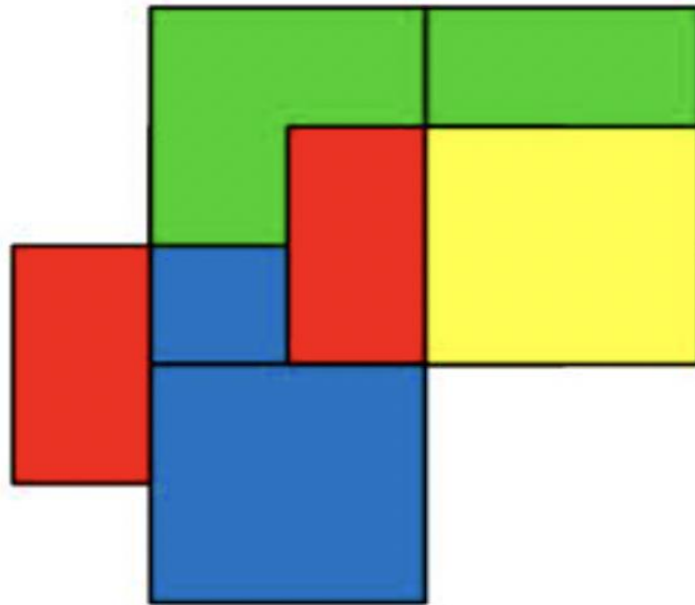
- ★ Snacks and drinks
- ★ Restroom? Bottle Filling Station?



# Tiled Area

<https://steveWyborne.com/2017/01/tiled-area-questions/>

**What is the area of this shape?**



# Connections

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## Domains

- Counting and Cardinality
- Operations and Algebra
- Numbers and Base Ten/  
Fractions

- Measurement (other areas)
  - Geometry
- 

# Perimeter and Area



The area of my garden is 20 feet.  
It is 4 feet long. How wide is my  
garden? (Factor unknown)

# 3 Act Task – Area with Fractional Units

- <https://gfletchy.com/the-big-pad/>

## Connections Domains

- Counting and Cardinality
- Operations and Algebra
- Numbers and Base Ten/  
Fractions
- Measurement (other areas)
- Geometry



# Is Capacity and Volume the same?

Give an example.

<https://www.youtube.com/watch?v=GKCE8ohIBqE>

The total amount of space  
an object occupies  
– hollow or solid

## Volume vs Capacity

The amount of a container  
can hold.  
– only hollow  
– Amount of something that can fit into a container  
• Solid, liquid or gas



Would you rather have Option A or Option B?

**OPTION  
A**

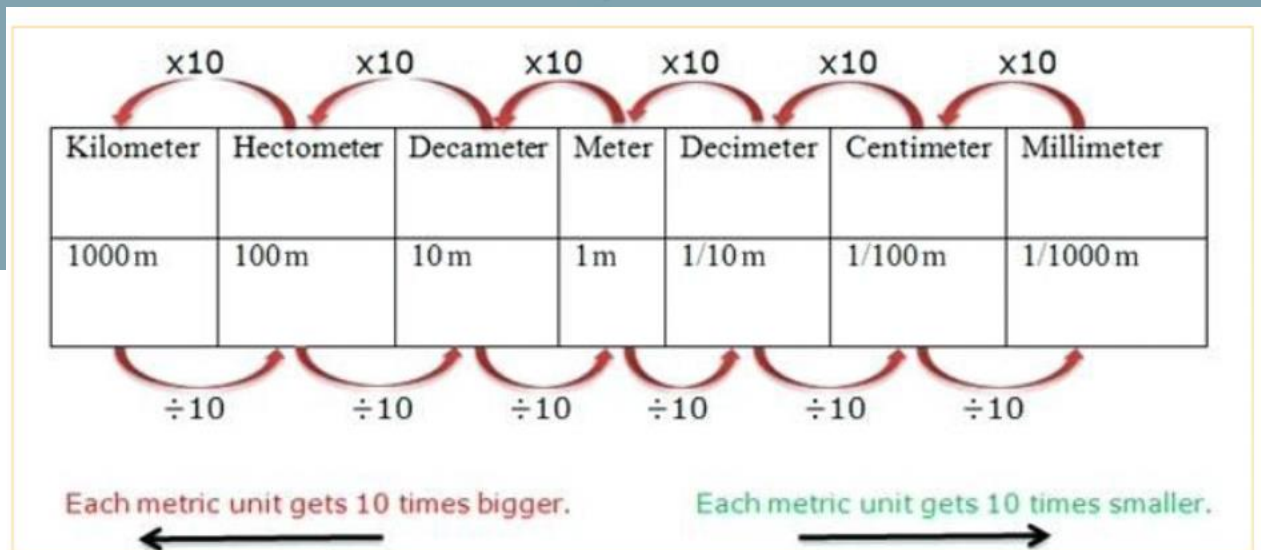


**A pitcher of 2 liters of  
lemonade**



**OPTION  
B**

**4 juice boxes with 250 mL  
of lemonade in each**



# Connections

## Domains

- Counting and Cardinality
- **Operations and Algebra**
- Numbers and Base Ten/  
Fractions
- Measurement (other areas)
- Geometry

$$1 \text{ lb} = 16 \text{ oz}$$

A baker is making a cake and needs to combine 3 pounds 12 ounces of flour with 2 pounds 10 ounces of sugar. How many pounds and ounces of flour and sugar will they have?



100

90

80

70

60

50

40

30

20

10

0



3 times as  
much orange  
as strawberry

In this diagram, quantities are represented on a measurement scale.



**Context matters!!!**

Do

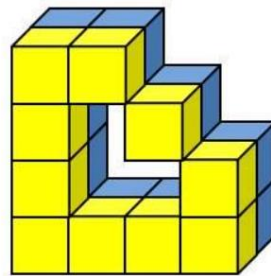
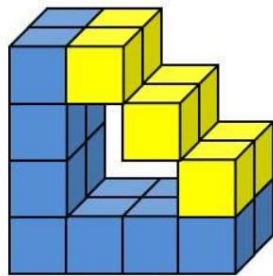
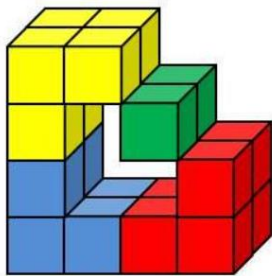
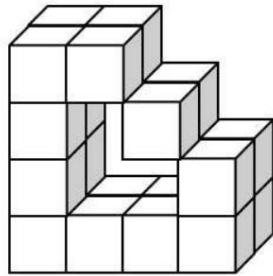
Lisa put two flavors of soda in a glass. There were 80 ml of soda in all. She put three times as much orange drink as strawberry. How many ml of orange did she put in? Prove it.





# Cube Conversions

<https://steveWyborne.com/?s=cube+conversations>



[Short Video to Explain](#)

<https://www.humix.com/video/KW4dz6aQBz2>

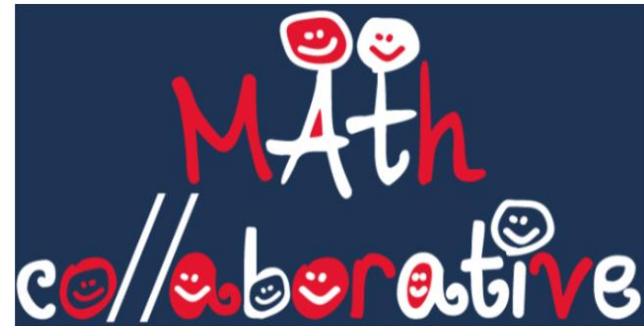


Share 1 take away.

What Questions do you have?

Thank you

for



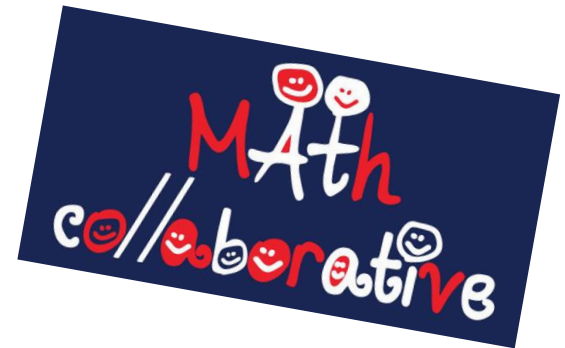
Making Connections with me!

[hensen\\_karen@columbusstate.edu](mailto:hensen_karen@columbusstate.edu)

# NOTES to NERDS



The official newsletter of the  
Collaborative



# reflect

*One or two key idea(s) or essential understanding that you hope to implement?*

**Math collaborative**

## How Did We Do?

Fill out this quick survey to receive your Professional Development Certificate!

*Survey for 6.5 Contact Hours*



**SCAN ME**